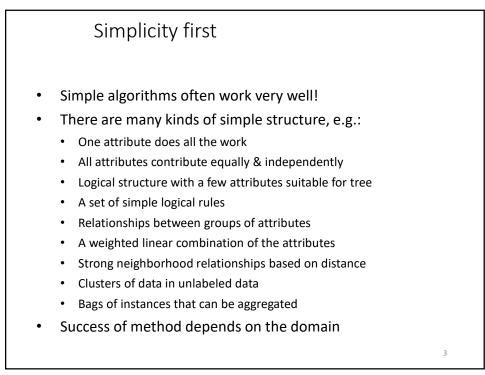
## Algorithms: The basic methods

Most of these slides (used with permission) are based on the book:

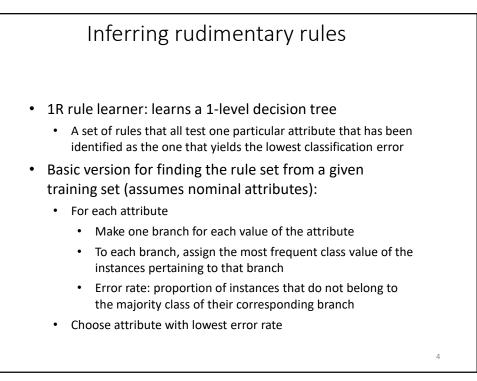
Data Mining: Practical Machine Learning Tools and Techniques by I. H. Witten, E. Frank, M. A. Hall, and C. J. Pal

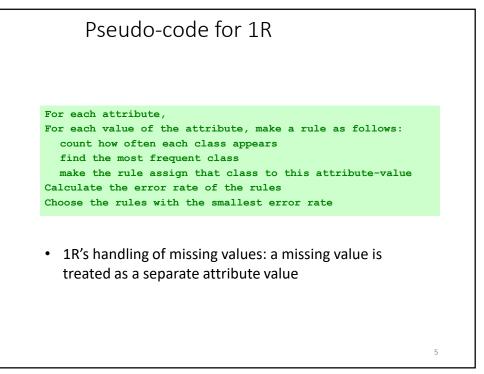
## Algorithms: The basic methods Inferring rudimentary rules Simple probabilistic modeling Constructing decision trees Constructing rules Association rule learning Linear models Clustering

2

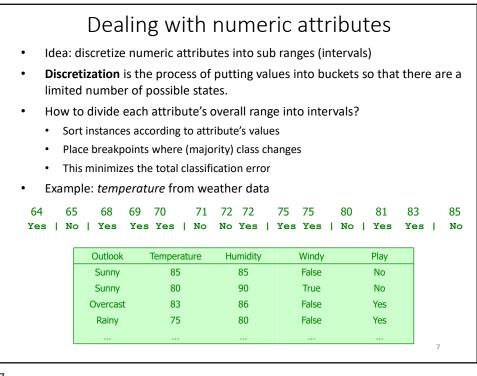






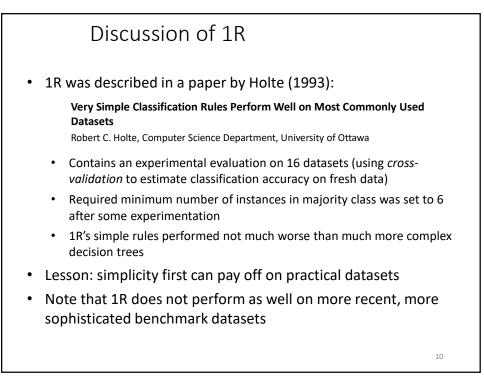


	E	valuat	ing t	hev	weathe	er attribute	es	
Outlook	Temp	Humidity	Windy	Play				
Sunny	Hot	High	False	No	Attribute	Rules	Errors	Total
Sunny	Hot	High	True	No	Outlook		2/5	errors 4/14
Overcast	Hot	High	False	Yes	OULIOOK	Sunny $\rightarrow$ No	2/5	4/14
Rainy	Mild	High	False	Yes		$Overcast \to Yes$	0/4	
Rainy	Cool	Normal	False	Yes		Rainy $\rightarrow$ Yes	2/5	
Rainy	Cool	Normal	True	No	Temp	$Hot \rightarrow No$	2/4	5/14
Overcast	Cool	Normal	True	Yes		$Mild \to Yes$	2/6	
Sunny	Mild	High	False	No		$Cool \rightarrow Yes$	1/4	
Sunny	Cool	Normal	False	Yes	Humidity	$High \to No$	3/7	4/14
Rainy	Mild	Normal	False	Yes		Normal $\rightarrow$ Yes	1/7	
Sunny	Mild	Normal	True	Yes	Windy	$False \to Yes$	2/8	5/14
Overcast	Mild	High	True	Yes		$True \to No$	3/6	
Overcast	Hot	Normal	False	Yes				
Rainv	Mild		True	No				
Railiy	MIIU	High	ITue	NU	J			
								6



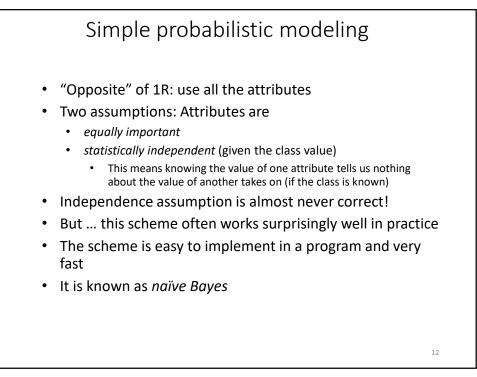
		The	e pi	robl	err	10	fov	erf	itti	ng					
• Sir en • Ex	A sir inter nple s <i>force i</i> ample	ation pr ngle insta val olution: minimu : tempe class se	ince w m nui ratur	vith an i mber o <u></u> re attrik	ncori f ins	rect o tanc	class lab es in m	el will ajorit	l prob ty cla	ss p	er il	nterva			s in
64 Yes	65 (р) No	68 🔊 Yes	69 Yes	70 Yes		72 №о	72 Yes 🕅	75 Yes	75 Yes		0 Io (	81 ¥es	83 Yes		85 No
64 Yes	65 No	68 Yes	69 Yes	70 Yes 🔇	71 No	72 No	72 Yes	75 Yes	75 Yes		0 Io	81 Yes	83 Yes		85 No
														8	

	ote tor the tour attribu	toc in th	o woothor
0	sets for the four attributes for the terms		
a, with only	two rules for the temp	Jerature	attribute.
Attribute	Rules	Errors	Total errors
Outlook	Sunny $\rightarrow$ No	2/5	4/14
	$Overcast \to Yes$	0/4	
	Rainy $\rightarrow$ Yes	2/5	
Temperature	$\leq$ 77.5 $\rightarrow$ Yes	3/10	5/14
	> 77.5 → No*	2/4	
Humidity	$\leq$ 82.5 $\rightarrow$ Yes	1/7	3/14
	> 82.5 and $\leq$ 95.5 $\rightarrow$ No	2/6	
	$> 95.5 \rightarrow \text{Yes}$	0/1	
Windy	$False \to Yes$	2/8	5/14
	True $\rightarrow$ No*	3/6	



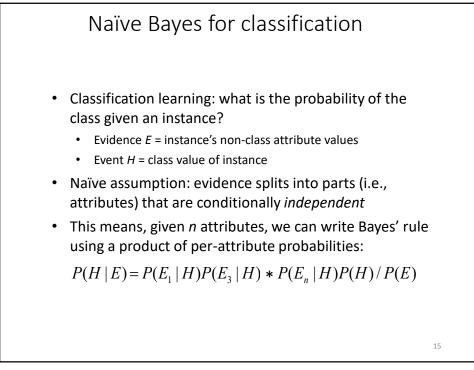
Weka Explorer		×
Preprocess Classify Cluster Associate	Belect attributes Visualize Auto-WEKA	
Choose OneR -B 6		
Choose Onex -B 6		
Test options	Classifier output	
Supplied test set Set. Cross-validation Folds 10 Percentage split % 90 More options (Nom) play Start Stop 21:24:05 - rules DecisionTable 21:22:04 - rules DecisionTable 21:22:23 - functions LinearRegression 21:32:23 - function LinearRegression 21:32:32 - function Li	Test mode: evaluate on training data Classifier model (full training set) outlookr mony -> No orescary (N/14 instances correct) Time taken to build model: 0 seconds Fraination on training set Time taken to test model on training data: 0 seconds Summary Correctly Classified Instances 10 71.4285 % Correctly Classified Instances 4 28.5714 % Magne statutic Monor relaymend error 0.5345 Relative absolute error 0.5345 Relative absolute error 111.4773 % Total Number of Instances 14	



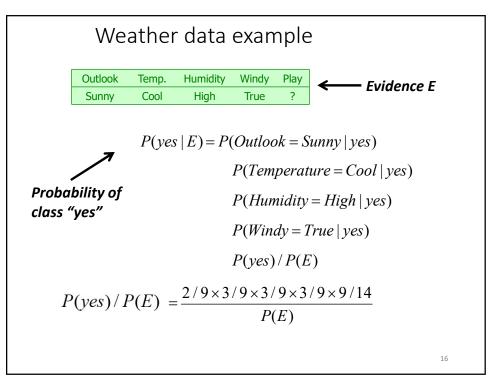


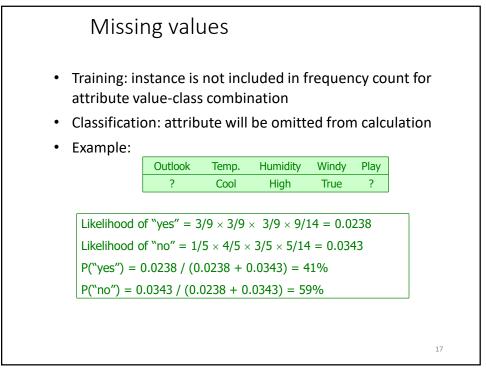
		Pr	oba	bili	ties	for w	veat	he	r dat	а			
Ou	itlook		Tempe	rature		Hu	umidity		V	/indy		Pla	ау
	Yes	No		Yes	No		Yes	No		Yes	No	Yes	No
Sunny	2	3	Hot	2	2	High	3	4	False	6	2	9	5
Overcast	4	0	Mild	4	2	Normal	6	1	True	3	3		
Rainy	3	2	Cool	3	1								
Sunny	2/9	3/5	Hot	2/9	2/5	High	3/9	4/5	False	6/9	2/5	9/	5/
Overcast	4/9	0/5	Mild	4/9	2/5	Normal	6/9	1/5	True	3/9	3/5	14	14
Rainy	3/9	2/5	Cool	3/9	1/5								
								Outloo		Hui Hig	nidity h	Windy False	Play No
								Sunny		Hig		True	No
								Overca	ist Hot	Hig	h	False	Yes
								Rainy	Mild	Hig		False	Yes
								Rainy	Cool		mal	False	Yes
								Rainy	Cool		mal	True	No
								Overca Sunny		Nor	mal b	True False	Yes No
								Sunny		-	mal	False	Yes
								Rainy	Mild	Nor	mal	False	Yes
								Sunny	Mild	Nor	mal	True	Yes
								Overca	st Mild	Hig	h	True	Yes
								Overca	ist Hot	Nor	mal	False	Yes
								Rainy	Mild	Hig	h	True	No

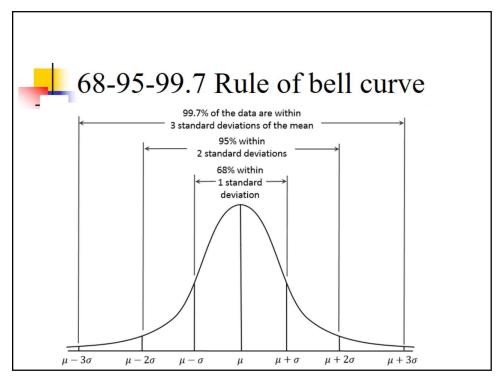
		Pr	obal	bilit	ies f	or we	athe	er c	lata				
O	utlook		Tempe	rature		Hu	midity			Windy		P	lay
	Yes	No		Yes	No		Yes	No		Yes	No	Yes	No
Sunny	2	3	Hot	2	2	High	3	4	False	6	2	9	5
Overcast	4	0	Mild	4	2	Normal	6	1	True	3	3		
Rainy	3	2	Cool	3	1								
Sunny	2/9	3/5	Hot	2/9	2/5	High	3/9	4/5	False	6/9	2/5	9/	5/
Overcast	4/9	0/5	Mild	4/9	2/5	Normal	6/9	1/5	True	3/9	3/5	14	14
Rainy	3/9	2/5	Cool	3/9	1/5								
	• A	new	day:		Outlook Sunny	Temp. Cool	Humi Hig	<u>,</u>	Windy True	Play ?			
						d of the two							
						"yes" = 2/9 "no" = 3/5	· · ·	· ·	1 ( ) ( ) ( ) ( ) ( ) ( ) ( ) ( ) ( ) (				
					Conversio	on into a pro	bability	by nor	malizati	on:			
					P(``)	/es") = 0.00	53 / (0.	0053 -	+ 0.0206	5) = 0.205	5		
					P(``r	no") = 0.020	06 / (0.0	053 +	0.0206	) = 0.795			
												14	

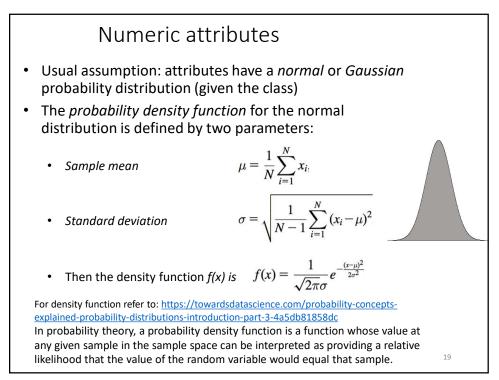


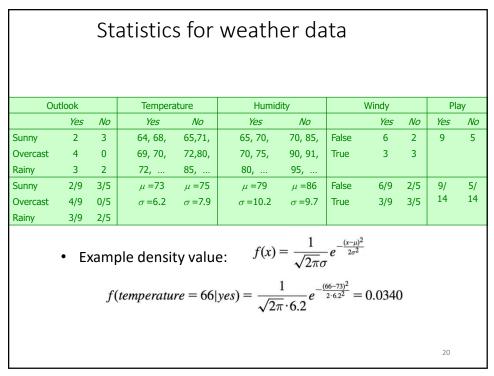


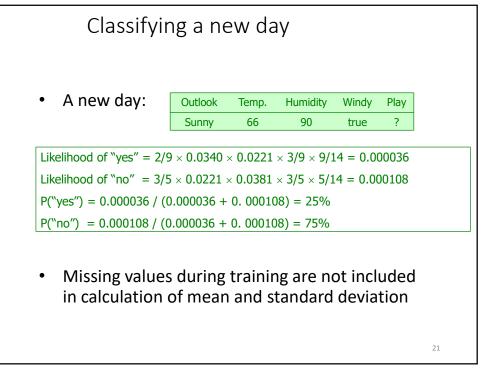


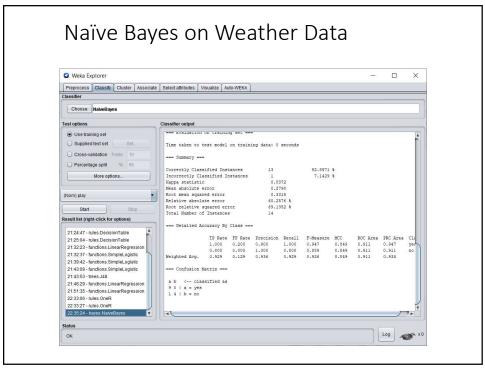


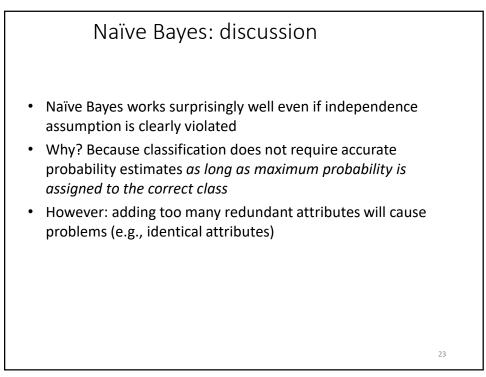


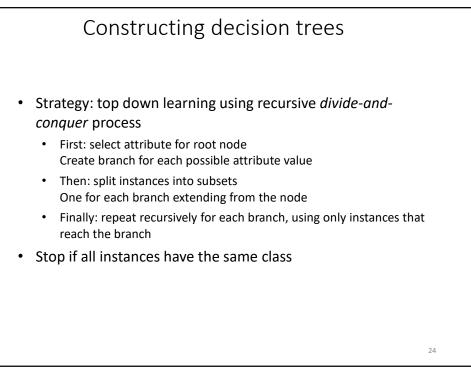


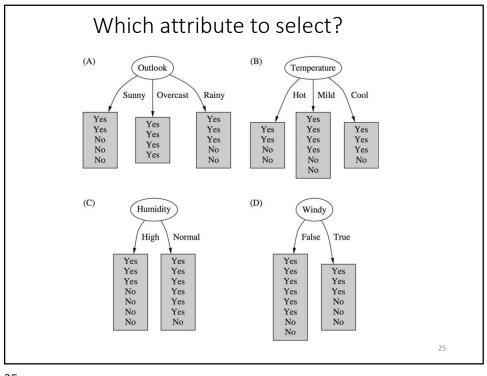


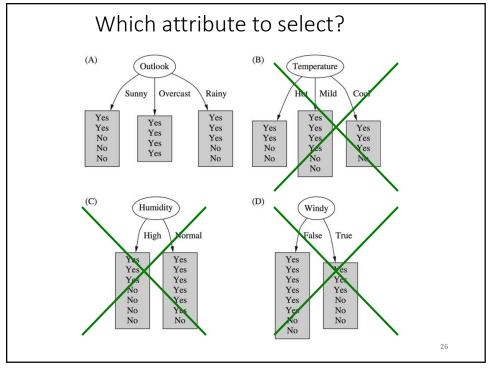








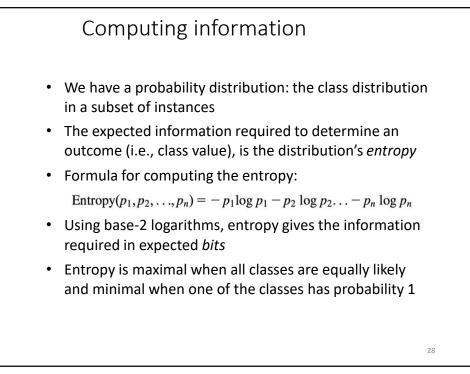


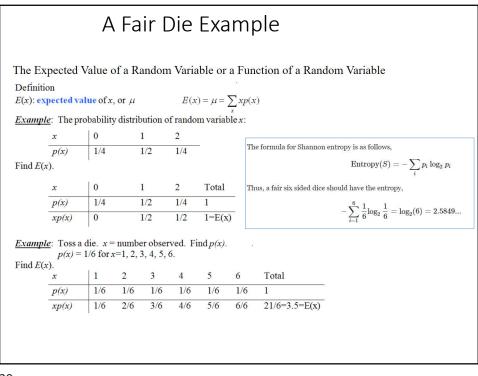


## Criterion for attribute selection

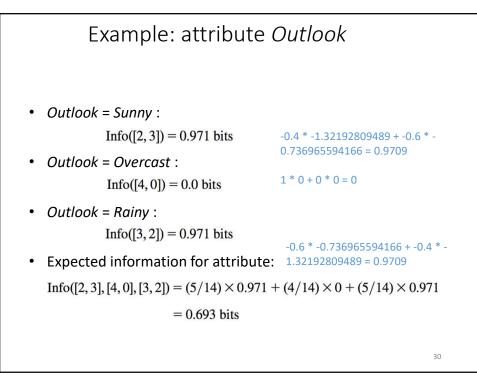
- Which is the best attribute?
  - Want to get the smallest tree
  - Heuristic: choose the attribute that produces the "purest" nodes
- Popular selection criterion: information gain
  - Information gain increases with the average purity of the subsets
- Strategy: amongst attributes available for splitting, choose attribute that gives greatest information gain
- Information gain requires measure of impurity
- Impurity measure that it uses is the *entropy* of the class distribution, which is a measure from information theory

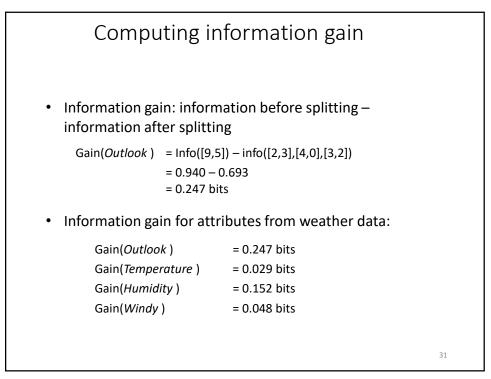
27

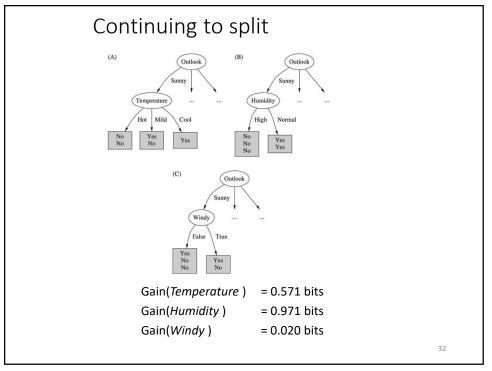


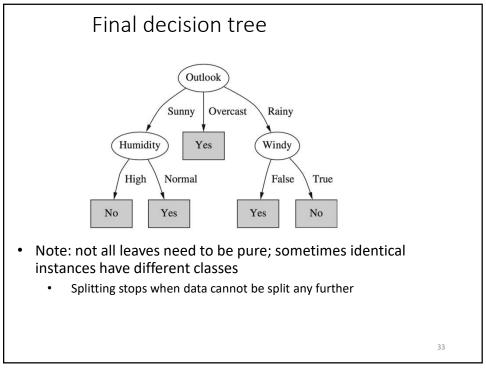




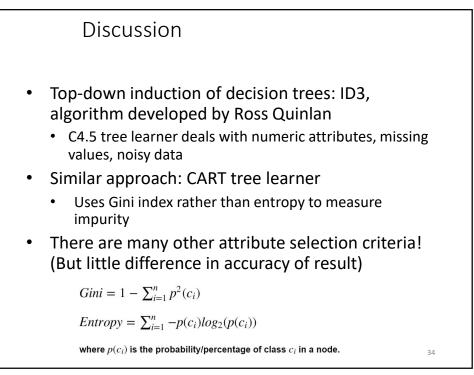


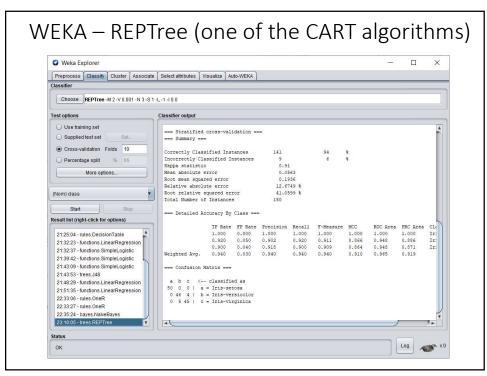


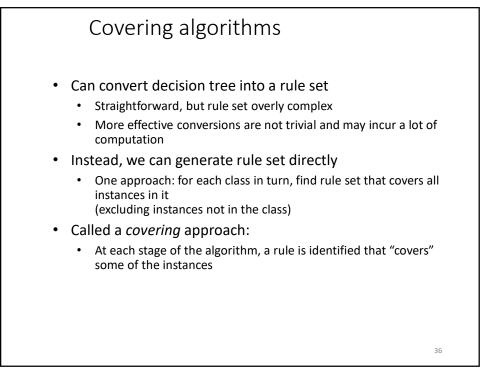


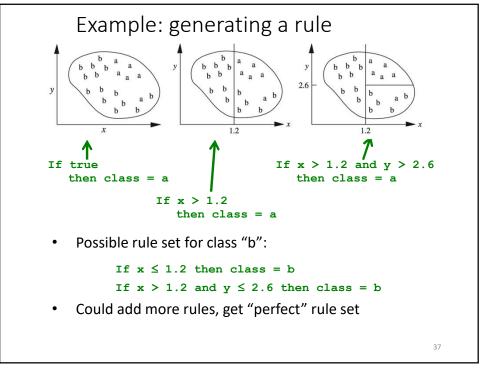


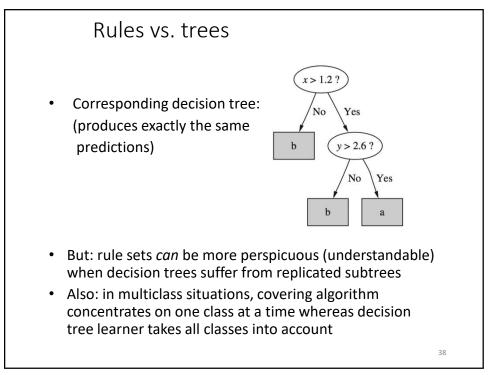


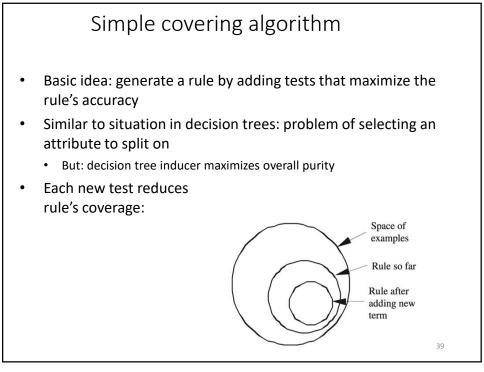


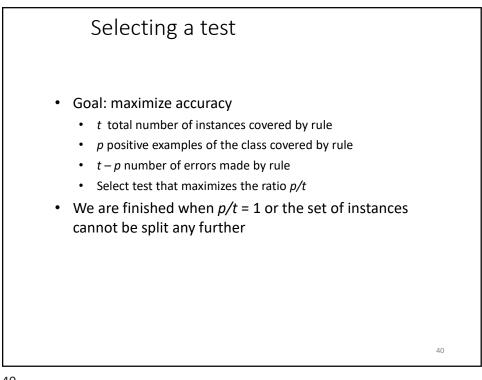








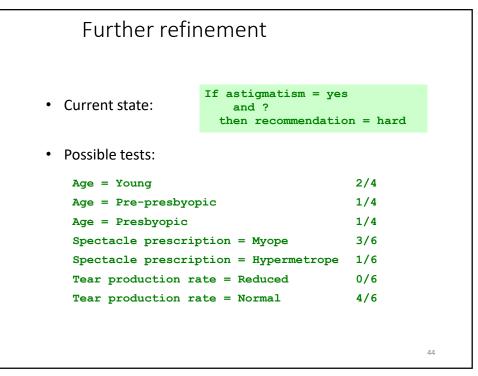




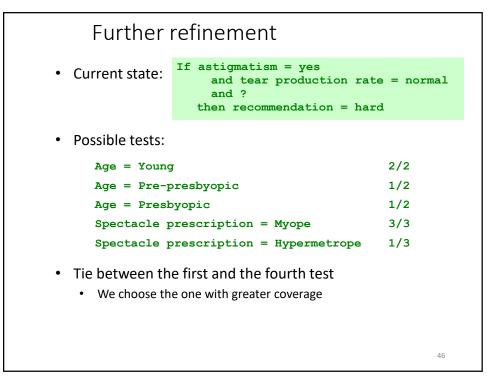
Age	Spectacle prescription	Astigmatism	Tear production rate	Recommended lenses
Young	Муоре	No	Reduced	None
Young	Муоре	No	Normal	Soft
Young	Myope	Yes	Reduced	None
Young	Муоре	Yes	Normal	Hard
Young	Hypermetrope	No	Reduced	None
Young	Hypermetrope	No	Normal	Soft
Young	Hypermetrope	Yes	Reduced	None
Young	Hypermetrope	Yes	Normal	hard
Pre-presbyopic	Муоре	No	Reduced	None
Pre-presbyopic	Муоре	No	Normal	Soft
Pre-presbyopic	Муоре	Yes	Reduced	None
Pre-presbyopic	Муоре	Yes	Normal	Hard
Pre-presbyopic	Hypermetrope	No	Reduced	None
Pre-presbyopic	Hypermetrope	No	Normal	Soft
Pre-presbyopic	Hypermetrope	Yes	Reduced	None
Pre-presbyopic	Hypermetrope	Yes	Normal	None
Presbyopic	Муоре	No	Reduced	None
Presbyopic	Муоре	No	Normal	None
Presbyopic	Муоре	Yes	Reduced	None
Presbyopic	Муоре	Yes	Normal	Hard
Presbyopic	Hypermetrope	No	Reduced	None
Presbyopic	Hypermetrope	No	Normal	Soft
Presbyopic	Hypermetrope	Yes	Reduced	None
Presbyopic	Hypermetrope	Yes	Normal	None

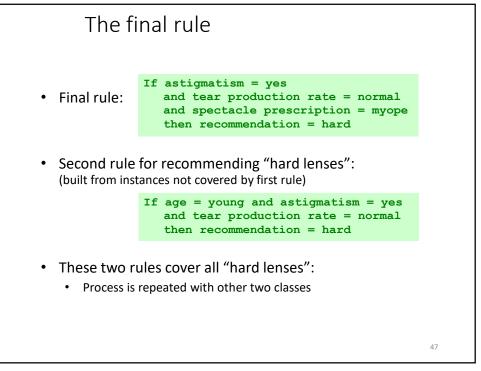
Exampl	e: contact lens data	
<ul><li> Rule we seek:</li><li> Possible tests:</li></ul>	<pre>If ?     then recommendation = har</pre>	d
Age = Your	ng	2/8
Age = Pre-	-presbyopic	1/8
Age = Pres	sbyopic	1/8
Spectacle	prescription = Myope	3/12
Spectacle	prescription = Hypermetrope	1/12
Astigmatis	sm = no	0/12
Astigmatis	sm = yes	4/12
Tear produ	action rate = Reduced	0/12
Tear produ	action rate = Normal	4/12
		42

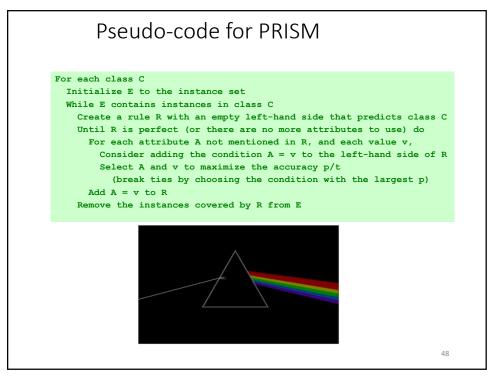
	Modified ru		resulting	data
	astigmatism = then recommen	ndation =		
• Insta Age	nces covered by Spectacle prescription		Tear production	Recommended
-	· · ·	-	rate	lenses
Young	Муоре	Yes	Reduced	None
Young	Муоре	Yes	Normal	Hard
Young	Hypermetrope	Yes	Reduced	None
Young	Hypermetrope	Yes	Normal	hard
Pre-presbyopic	Муоре	Yes	Reduced	None
Pre-presbyopic	Муоре	Yes	Normal	Hard
Pre-presbyopic	Hypermetrope	Yes	Reduced	None
Pre-presbyopic	Hypermetrope	Yes	Normal	None
Presbyopic	Муоре	Yes	Reduced	None
Presbyopic	Муоре	Yes	Normal	Hard
Presbyopic	Hypermetrope	Yes	Reduced	None
Presbyopic	Hypermetrope	Yes	Normal	None
				43

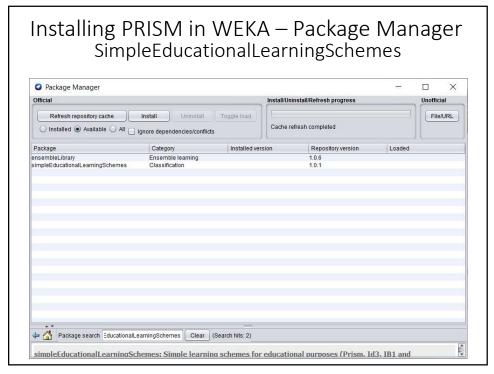


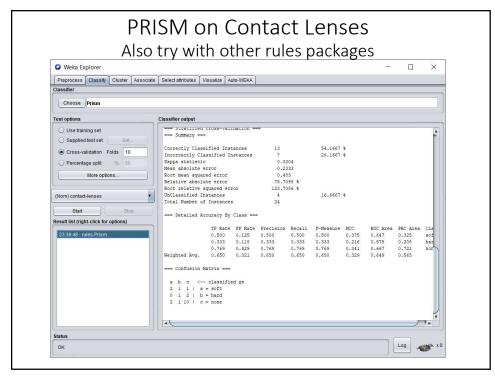
I	Modified ru	le and	resulting o	data
• Rule	with best test ac	ded:		
	If astigmatism and tear p then recommend	roduction	rate = normal rd	
• Insta	nces covered by	modified r	ule:	
4.50		Actignation	Toor production	Decommonded
Age	Spectacle prescription	Astigmatism	Tear production	Recommended
	Spectacle prescription	Astigmatism	Tear production rate Normal	Recommended lenses Hard
Young	Spectacle prescription Myope		rate	lenses
	Spectacle prescription	Yes	rate Normal	lenses Hard
Young Young	Spectacle prescription Myope Hypermetrope	Yes Yes	rate Normal Normal	lenses Hard hard
Young Young Pre-presbyopic	Spectacle prescription Myope Hypermetrope Myope	Yes Yes Yes	rate Normal Normal Normal	lenses Hard hard Hard
Young Young Pre-presbyopic Pre-presbyopic	Spectacle prescription Myope Hypermetrope Myope Hypermetrope	Yes Yes Yes Yes	rate Normal Normal Normal Normal	lenses Hard hard Hard None

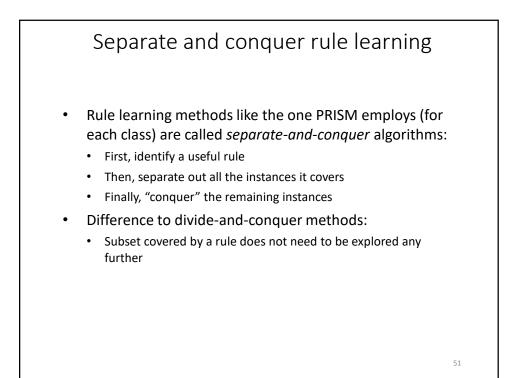


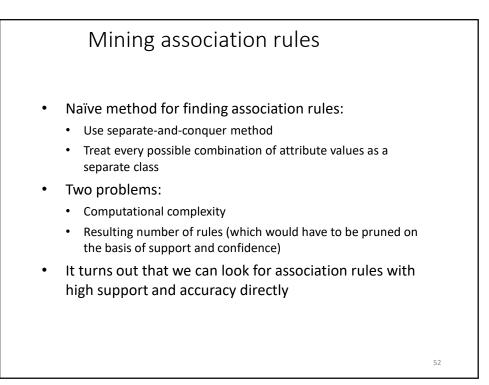


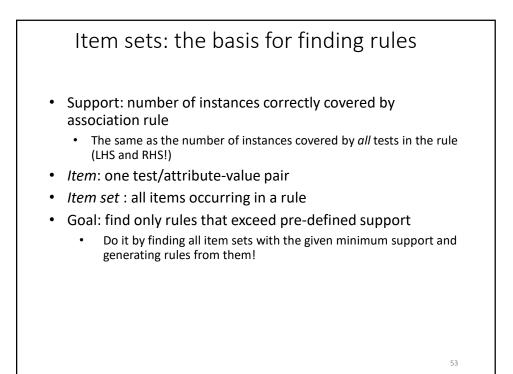




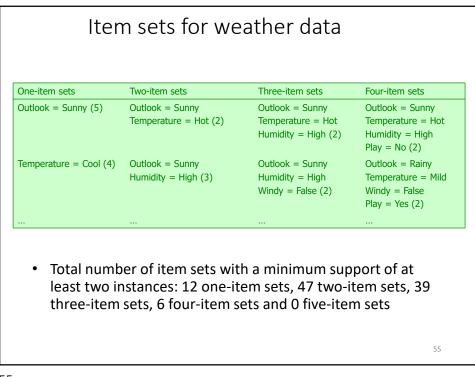


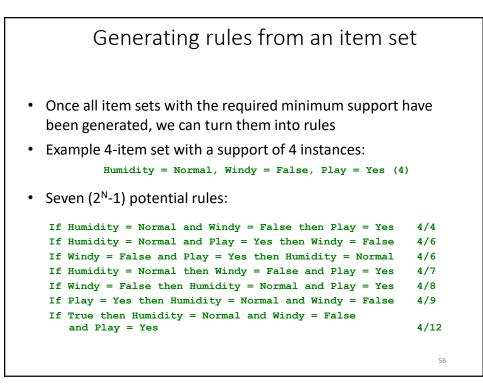


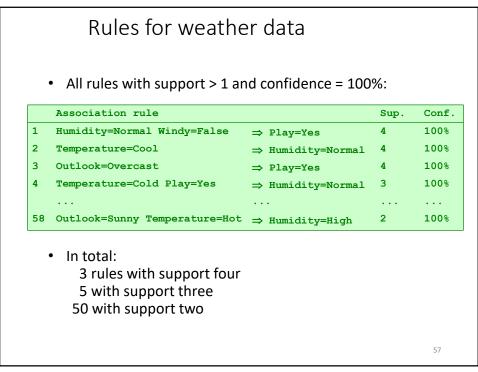


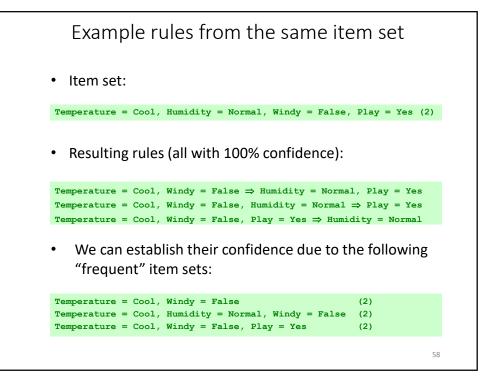


'eather	<sup>-</sup> data				
Outlook	Temp	Humidity	Windy	Play	
Sunny	Hot	High	False	No	
Sunny	Hot	High	True	No	
Overcast	Hot	High	False	Yes	
Rainy	Mild	High	False	Yes	
Rainy	Cool	Normal	False	Yes	
Rainy	Cool	Normal	True	No	
Overcast	Cool	Normal	True	Yes	
Sunny	Mild	High	False	No	
Sunny	Cool	Normal	False	Yes	
Rainy	Mild	Normal	False	Yes	
Sunny	Mild	Normal	True	Yes	
Overcast	Mild	High	True	Yes	
Overcast	Hot	Normal	False	Yes	
Rainy	Mild	High	True	No	



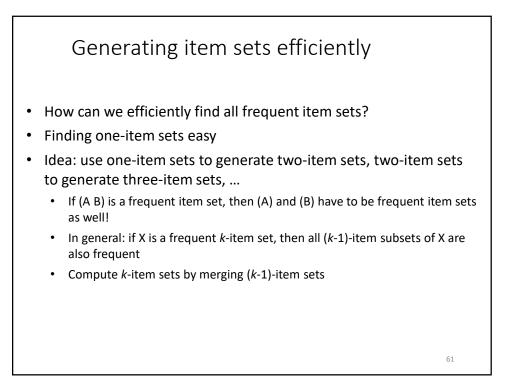


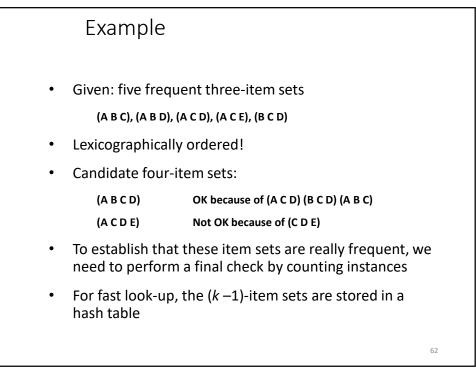




ssociator	Cluster Associate Select attributes Visualize Auto-WEKA Forecast			
	-N 10 -T 0 -C 0.9 -D 0.05 -U 1.0 -M 0.1 -S -1.0 -A -c 5			
Start Stop	Associator output			
esult list (right-cli	Run information			
2:30:34 - Apriori 2:31:25 - Apriori	Scheme: weka.associations.Apriori -N 10 -T 0 -C 0.9 -D 0.05 -U 1.0 Relation: weather.symbolic	weka.gui.Generic	ing set concern the set	
2:31:41 - Apriori	Instances: 14 Attributes: 5	weka.associations.Aprior	i	
	outlook temperature	About Class implementing an	Apriori-type algorithm. More	
	humidity	course ingrementing an	Capabilities	
	windy play	l		
	=== Associator model (full training set) ===		True	
	Apriori	classIndex		
			0.05	
	Minimum support: 0.1 (l instances) Minimum metric <confidence>: 0.9</confidence>	doNotCheckCapabilities	False 👻	
	Number of cycles performed: 18	lowerBoundMinSupport	0.1	
	Generated sets of large itemsets:	metricType	Confidence	
	Size of set of large itemsets L(1): 17	minMetric	0.9	
	Size of set of large itemsets L(2): 27	numRules	10	
	Size of set of large itemsets L(3): 6	outputitemSets	False 💌	
	Best rules found:	removeAllMissingCols	False 💌	
	1. outlook=overcast 4 ==> play=yes 4 conf:(1)	significanceLevel	-1.0	
	2. humidity=normal windy=FALSE 4 ==> play=yes 4 conf:(1) 3. outlook=sunny humidity=high 3 ==> play=no 3 conf:(1)	treatZeroAsMissing	False	
	4. outlook=rainy windy=FALSE 3 ==> play=yes 3 conf: (1) 5. outlook=sunny humidity=normal 2 ==> play=yes 2 conf: (1)	upperBoundMinSupport	1.0	
	6. outlook=sunny temperature=hot 2 ==> play=no 2 conf: (1) 7. outlook=overcast temperature=hot 2 ==> play=yes 2 conf: (1)	verbose	False	
	8. outlook=overcast humidity=high 2 ==> play=yes 2 conf:(1)			
	<pre>10. outlook=overcast windy=TRUE 2 ==&gt; play=yes 2 conf:(1) 10. outlook=overcast windy=TRUE 2 ==&gt; play=yes 2 conf:(1)</pre>	Open	Save OK Cancel	
	9. outlook=overcast humidity=normal 2 ==> play=yes 2 conf:(1)	Open	Save OK Cancel	

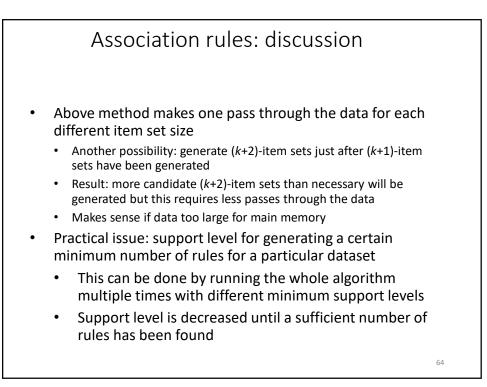
Weka Explorer					
	Cluster Associate Select attributes Visualize	Auto-WEKA   Forecast			
Associator Choose Apriori -	-N 10 -T 0 -C 0.9 -D 0.05 -U 1.0 -M 0.05 -S -1.0	-A -c 217			
Start Stop	Associator output				
Result list (right-cli	Attributes: 217 (list of attributes cmit	tedl			
22:30:34 - Apriori	Associator model (full training as	ann (25	11.11		
22:31:25 - Apriori 22:31:41 - Apriori		weka.gui.Generic	ObjectEditor	×	
22:34:11 - Apriori	Apriori	weka.associations.Apriori	1		
22:35:07 - Apriori	Minimum support: 0.05 (231 instances)	About			
	Minimum metric <confidence>: 0.9</confidence>	Class implementing an	Apriori-type algorithm.	More	
	Number of cycles performed: 19			Capabilities	
	Generated sets of large itemsets:	car	True	*	r i
	Size of set of large itensets L(1): 9	classIndex	217		
	Size of set of large itemsets L(2): 1	delta	0.05		
	Size of set of large itemsets L(3): 4	doNotCheckCapabilities	False	*	
	Size of set of large itensets L(4): 1	lowerBoundMinSupport	0.05		
	Size of set of large itemsets L(S): 1	metricType		*	
	Size of set of large itemsets L(6): 1	minMetric	1		
	Size of set of large itemsets L(7): 3	numRules			
	Size of set of large itemsets L(8): 4	outputItemSets		Ŧ	
	Size of set of large itemsets L(9); 1	removeAllMissingCols		*	
	Best rules found:				
		significanceLevel			
	<ol> <li>bread and cake=t juice-sat-cord-m</li> <li>baking needs=t sauces-gravy-pkle=</li> </ol>	treatZeroAsMissing	1	*	<pre>sgetables=t 249 ==&gt; total=high 235 conf:(0.94) =&gt; total=high 238 conf:(0.93)</pre>
	<ol> <li>bread and cake=t sauces-gravy-pkl</li> <li>bread and cake=t baking needs=t j</li> </ol>	upperBoundMinSupport	1.0		*> total=high 237 conf:(0.93) tissues-paper prd=t 253 ==> total=high 235 conf:(0.93)
	<ol> <li>bread and cake=t juice-sat-cord-m</li> <li>bread and cake=t baking needs=t to</li> </ol>	verbose	False	*	<pre>it=t vegetables=t 253 ==&gt; total=high 235</pre>
	7. biscuits=t sauces-gravy-pkle=t fr				251 ==> total=high 233 conf:(0.93)
	<ol> <li>bread and cake-t biscuits-t sauce</li> <li>biscuits=t sauces-gravy-pkle=t from the sauces sauces</li></ol>	Open	Save OK	Cancel	t 250> total-high 232 conf:(0.93)
					ese-t margarine=t 256 ==> total=high 237 conf:(0.93)
	4				

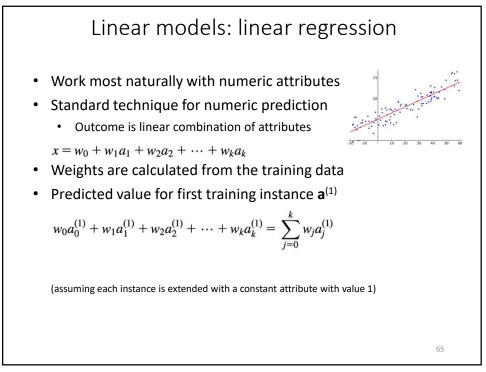


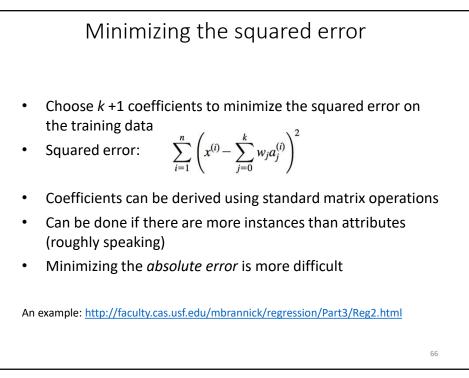


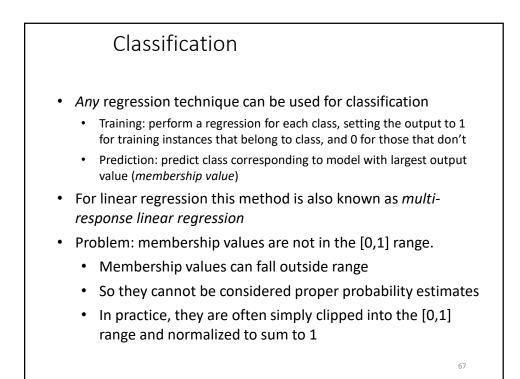
## Algorithm for finding item sets

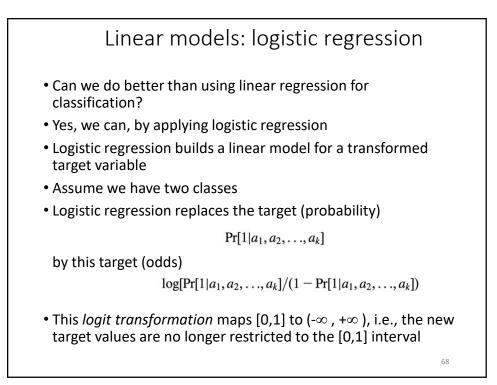
```
Set k to 1
Find all k-item sets with sufficient coverage and store them in hash table #1
While some k-item sets with sufficient coverage have been found
Increment k
Find all pairs of (k-1)-item sets in hash table #(k-1) that differ only in
their last item
Create a k-item set for each pair by combining the two (k-1)-item sets
that are paired
Remove all k-item sets containing any (k-1)-item sets that are not in the
#(k-1)hash table
Scan the data and remove all remaining k-item sets that do not have
sufficient coverage
Store the remaining k-item sets and their coverage in hash table #k,
sorting items in lexical order
```

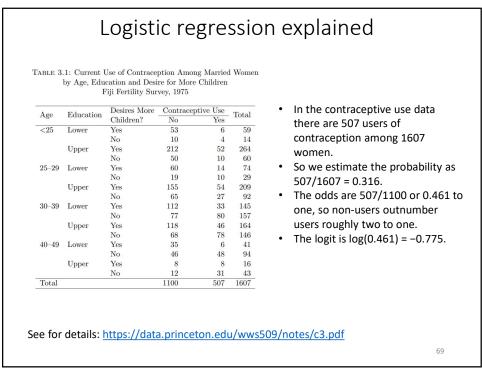




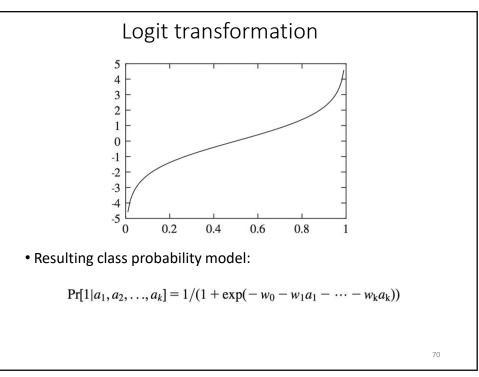


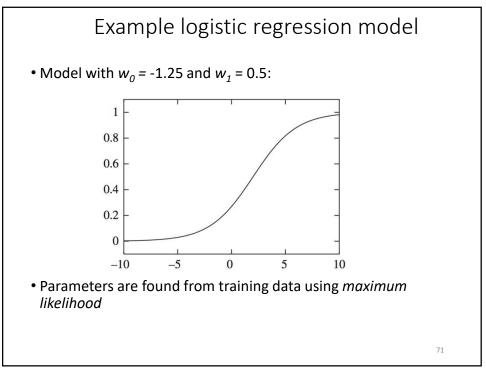


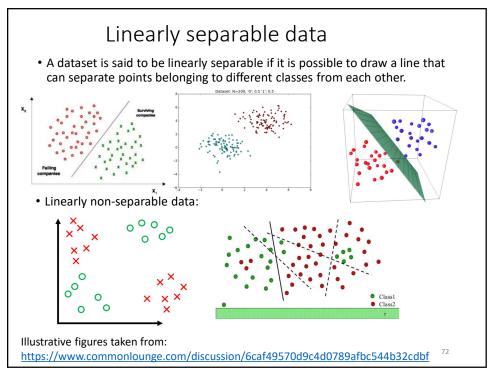


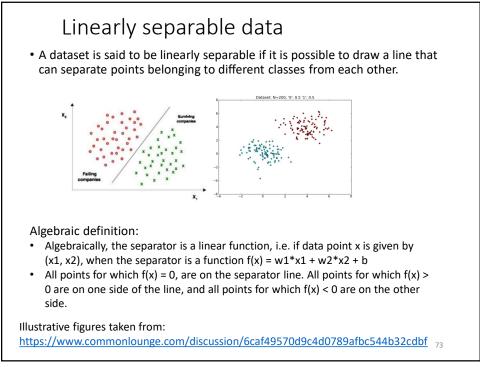




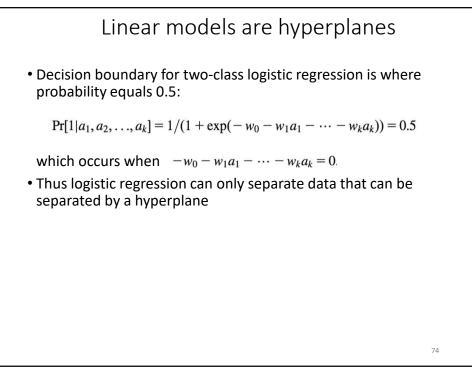


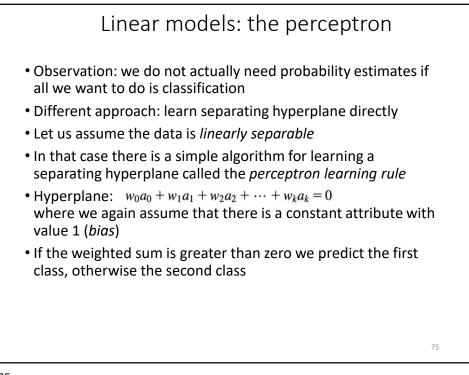




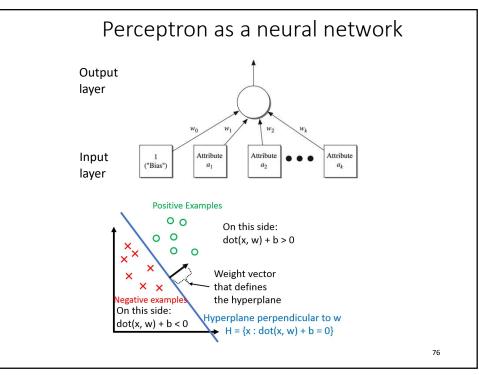


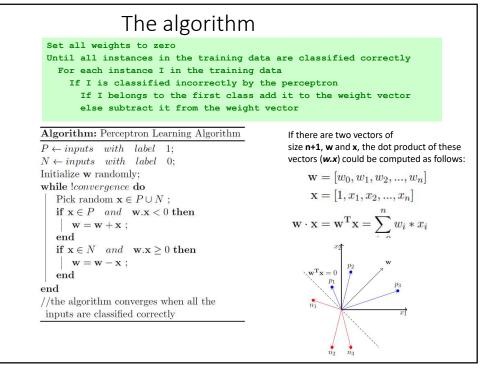






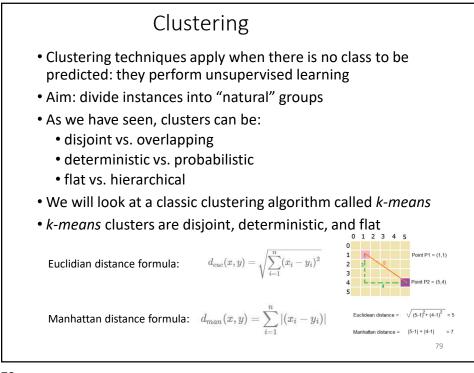




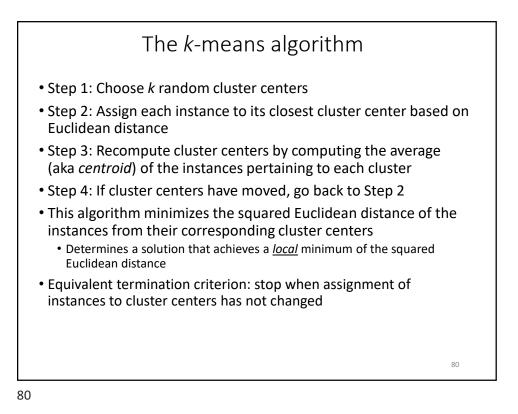


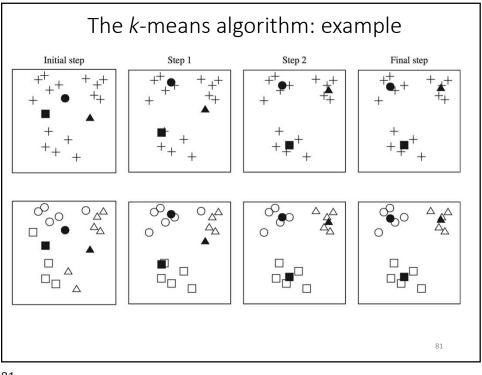


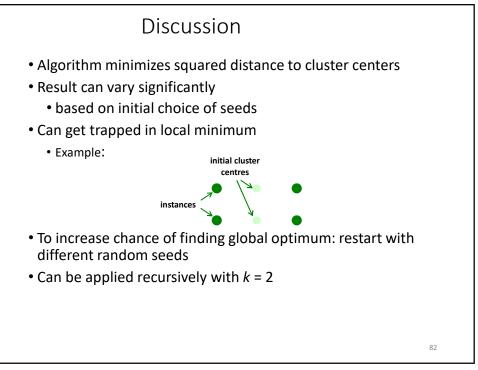
G Weka Explorer								8 <del></del> 8		×
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(Nom) class	Relative absolute error Root relative squared error Total Number of Instances		27.3796 % 150							
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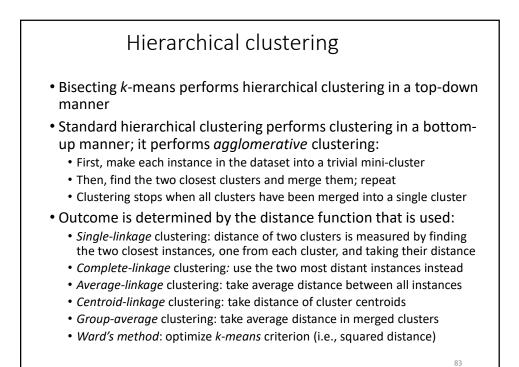




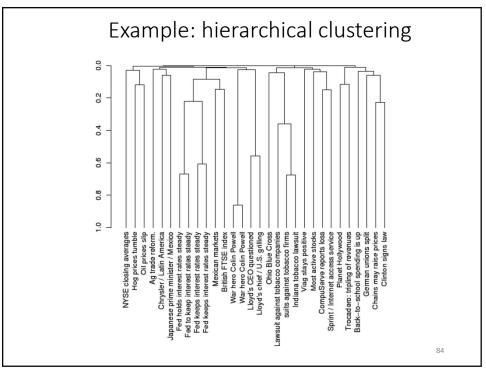


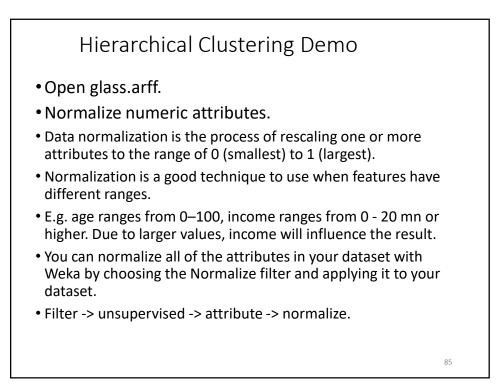


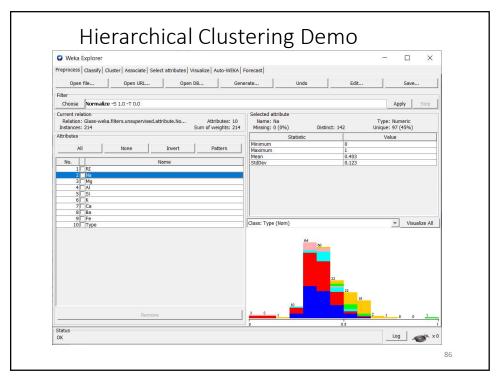












Clusterer	Select attributes   Visualize   Auto-WEKA   Forecast   6-L. SPV2LE - A *weka.cone.Euclidear/Distance -R first-last* Clusterer output	
Use training set	Clusterer output	
C Percentage split % C Classes to clusters evaluation (Nom) Type IStore clusters for visualization Ignore attributes	veka.gui.GenericObjectEditor     veka.duterers.HierarchicalClusterer     About     Hierarchical dustering class.     More     Capabilities	
Start Stop Result list (right-click for options)	debug     False     *       distanceFunction     Choose     EuclideanDistance -R frst-last       distanceIsBranchLength     False     *       dototCheckCapabilities     False     *       lmkType     SINGLE     *       munClusters     6     *       printflework     True     *	
	Open  OK  Cancel	



