



Binomial example

Take the example of 5 coin tosses. What's the probability that you flip exactly 3 heads in 5 coin tosses?

3

Binomial distribution

Solution:

One way to get exactly 3 heads: HHHTT

What's the probability of this <u>exact</u> arrangement? P(heads)xP(heads) xP(heads)xP(tails)xP(tails) $=(1/2)^3 x (1/2)^2$

Another way to get exactly 3 heads: THHHT Probability of this exact outcome = $(1/2)^1 x (1/2)^3 x (1/2)^2$









Binomial distribution, generally

Note the general pattern emerging \rightarrow if you have only two possible outcomes (call them 1/0 or yes/no or success/failure) in *n* independent trials, then the probability of exactly X "successes"=



























$$p(X=k) = \frac{\pi e}{k!}$$













1a. If calls to your cell phone are a Poisson process with a constant rate $\lambda=2$ calls per hour, what's the probability that, if you forget to turn your phone off in a 1.5 hour movie, your phone rings during that time? X ~ Poisson ($\lambda=2$ calls/hour)

 $P(X \ge 1) = 1 - P(X = 0)$

$$P(X=0) = \frac{(2*1.5)^{0} e^{-2(1.5)}}{0!} \frac{(3)^{0} e^{-3}}{0!} = e^{-3} = .05$$

∴ P(X≥1)=1 – .05 = 95% chance

1b. How many phone calls do you expect to get during the movie?

 $E(X) = \lambda t = 2(1.5) = 3$